

Describing the ocean variability as an atmospherically-modulated oceanic "chaos"

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CNRS - IGE

OCCIPUT project
OceaniC Chaos – ImPacts, strUcture, predicTability

Thanks to

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Yan, B.I. Garcia-Gomez, G. Fedele, A.
Colella, S. Pierini, S. Cravatte, W.
Llovel, A. Hogg, L. Zanna ...

Sea level chaotic variability
($T > 2$ yr, $L > 1200$ km)
From -5 cm to +5 cm

Idealized models : Low-Freq (LF) Chaotic Intrinsic Variability (CIV)

Constant/seasonal wind forcing : Increased $Re \rightarrow$

Spontaneous emergence of LF CIV (1-10 year)

Dijkstra & Ghil 2005; Sushama et al 2007; etc

■ Western boundary current systems

- Surface jets, DWBC, Recirculation gyres (shape, strength)

Dewar 2003; Spall 1996; etc

- Mode waters (low-PV pool volume)

- Rossby modes

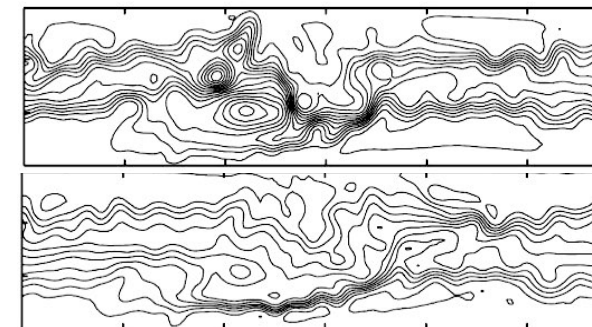
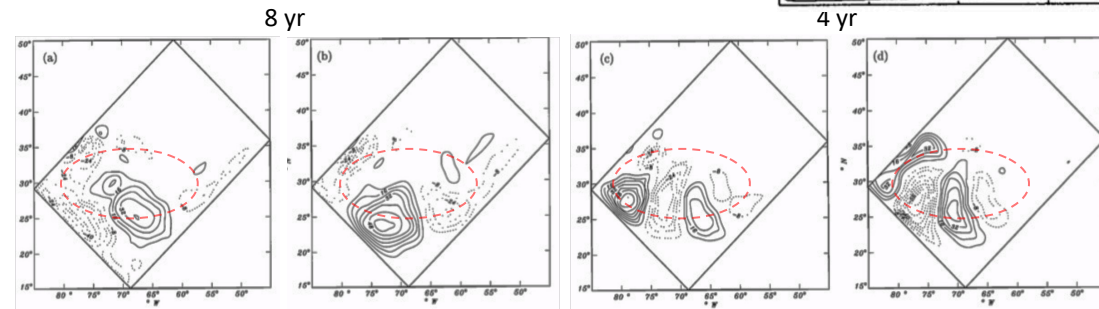
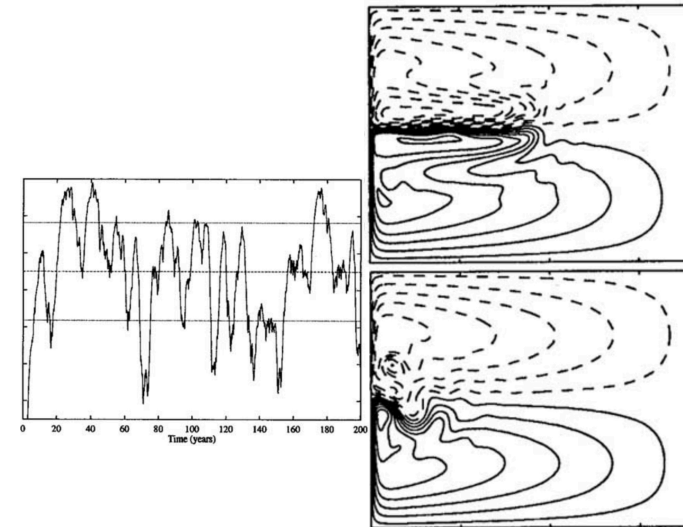
Hazeleger & Drijfhout 2000; etc

■ ACC Current / eddy / topography interactions

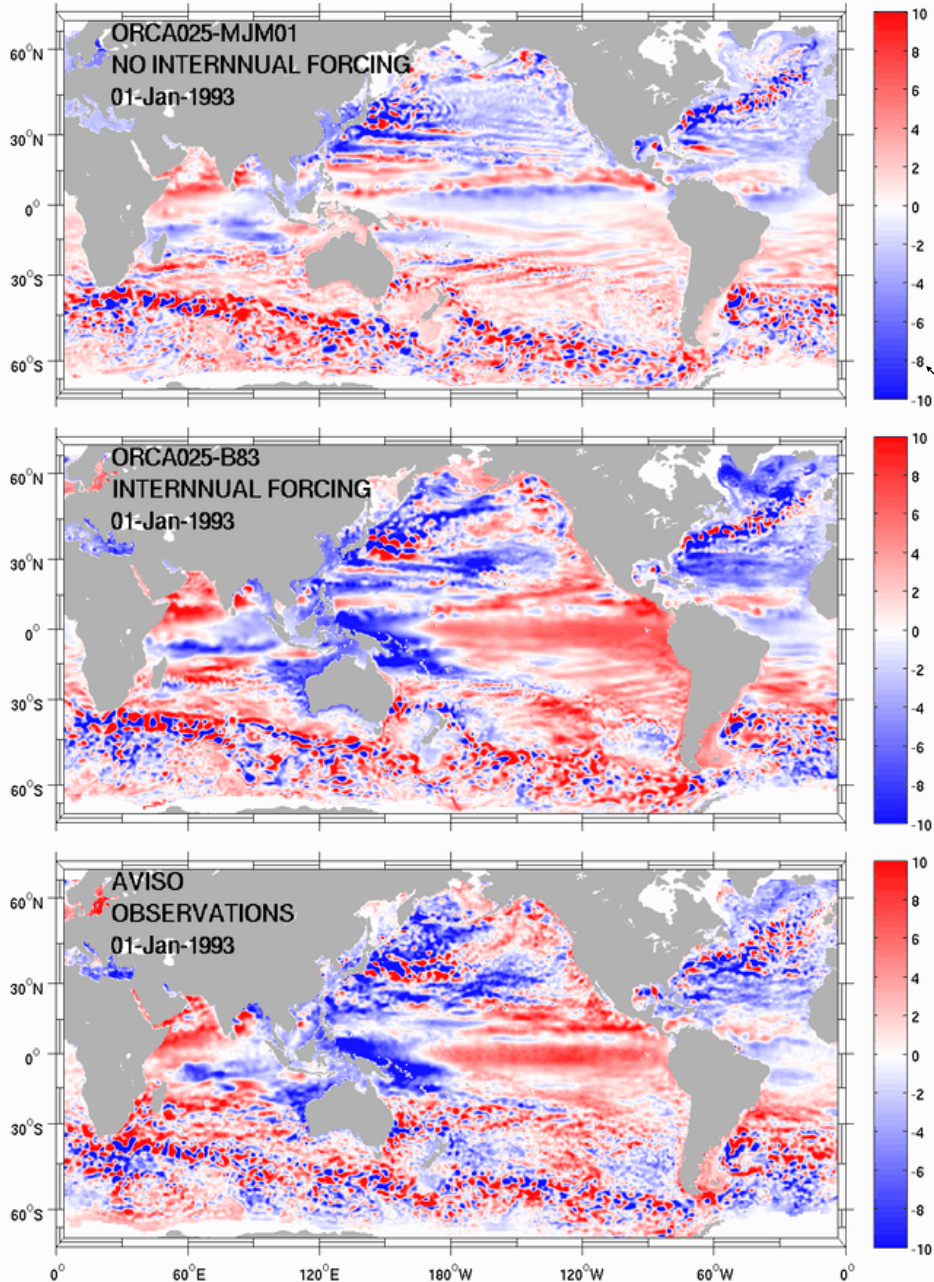
- path, transport

- jet jumping & migration

Hogg & Blundell 2006; Thompson & Richards 2011; Chapman & Hogg 2013; etc



Global PE model : Low-Freq (LF) Chaotic Intrinsic Variability (CIV)



Imprints of CIV & atmospheric variability in a global OGCM?
Keeping the link with observations and idealized & theoretical work

Penduff et al (2011)
Gregorio et al (2015)
Serazin et al (2015)

Interannual SLA anomalies (LF CIV) in

NEMO 1/4° driven by:

- Seasonal forcing

1) Comparable to idealized models in structures & scales

2) Comparable in amplitude (mid-lat & ACC) to :

- Fully-variable forcing

Altimeter observations

Assessing roles of CIV & atmospheric variability in the ocean

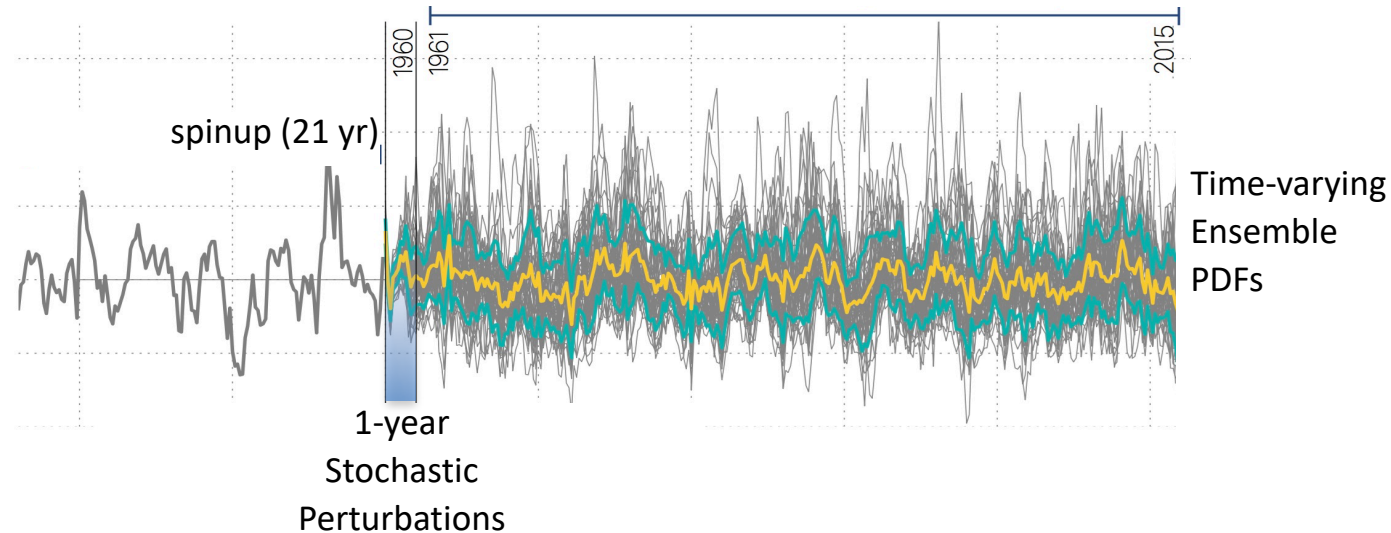
OCCIPUT ENSEMBLE OCEAN SIMULATION

<https://meom-group.github.io/projects/occiput/>

50 members, same realistic forcing (~ERA-interim)

Initial perturbations → 56 year integration (1960-2015)

Global ocean-sea ice
NEMO model. $\Delta = 1/4^\circ$



Penduff et al (2014)
Bessières et al (2017)
Leroux et al (2018)

1. Separating CIV and atmospherically-forced variability

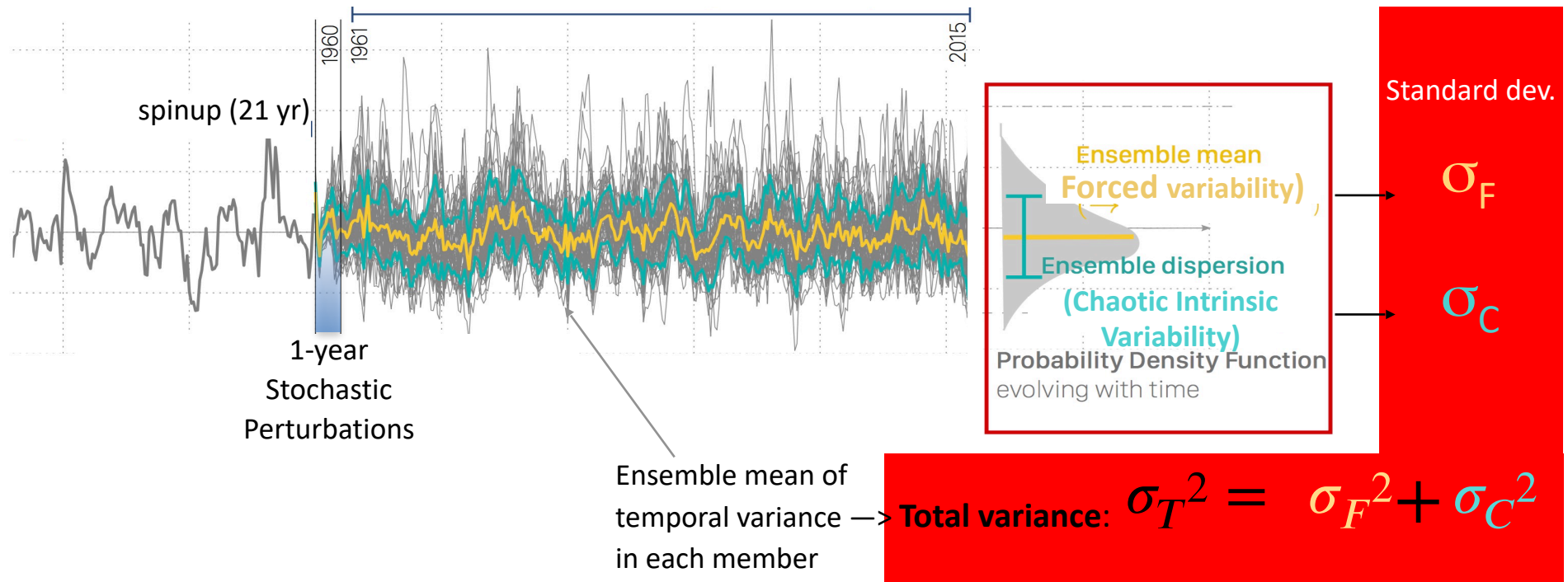
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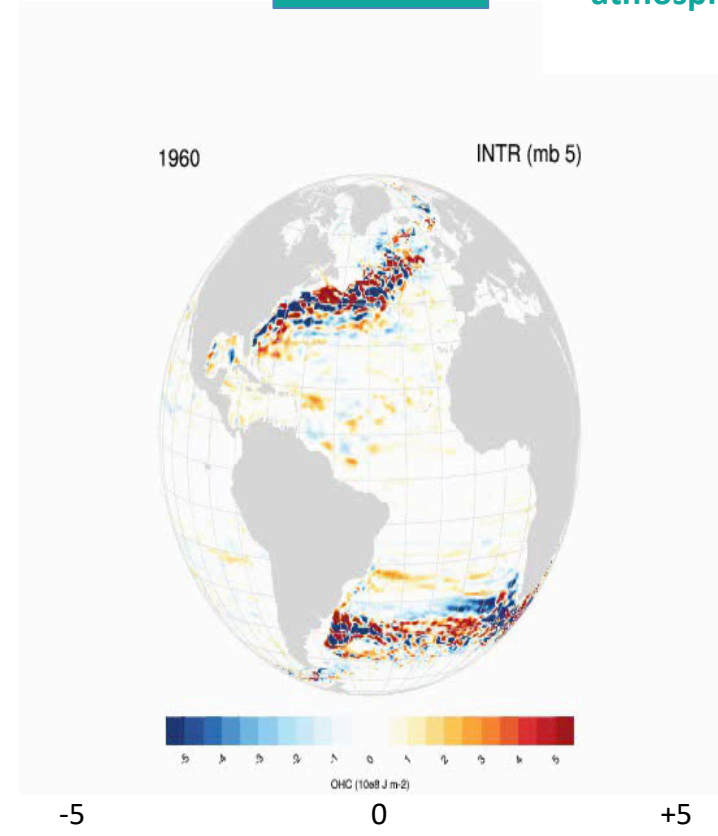
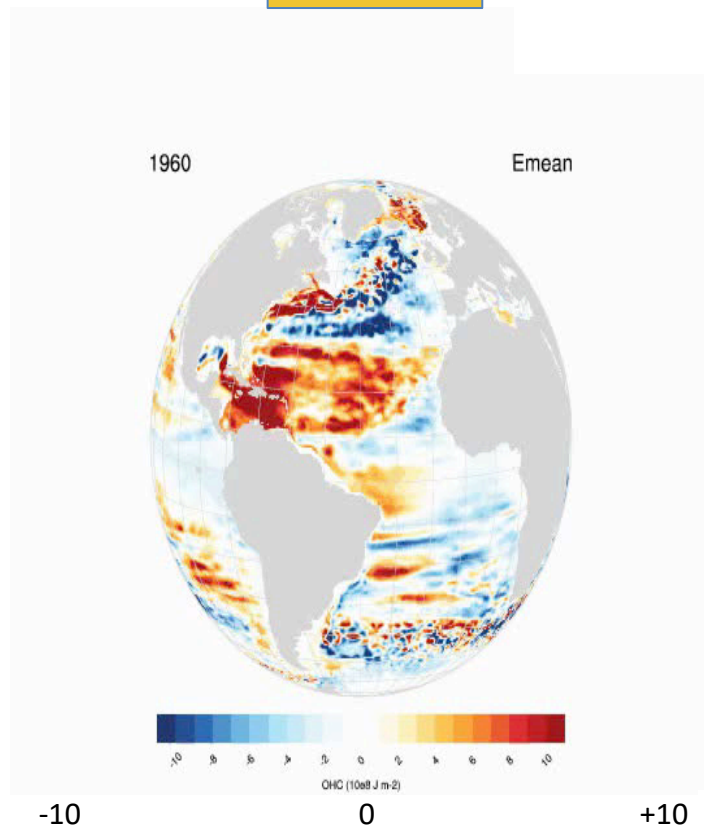
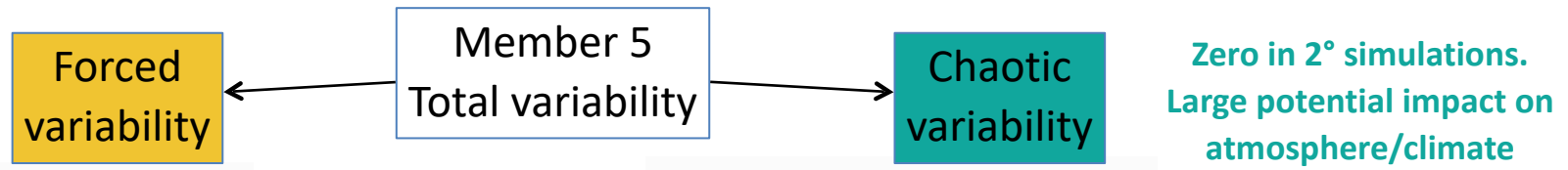
Penduff et al (2014)
Bessières et al (2017)
Leroux et al (2018)

I.

Separating
Forced / chaotic
variability

OHC_{0-700m} : Forced & Chaotic 2-18 yr variability

$$OHC = \rho \cdot C_p \int_{-700}^{surf} T(z) \cdot dz \quad yr = 1980, 2010 \quad member = 1, 50$$



OHC_{0-700m} : Forced & Chaotic 2-18 yr variability

$$OHC = \rho \cdot C_p \int_{-700}^{surf} T(z) \cdot dz \quad yr = 1980, 2010 \quad member = 1,50$$

E_{mean} (T_{std})



Total STD

T_{std} (E_{mean})



Forced STD

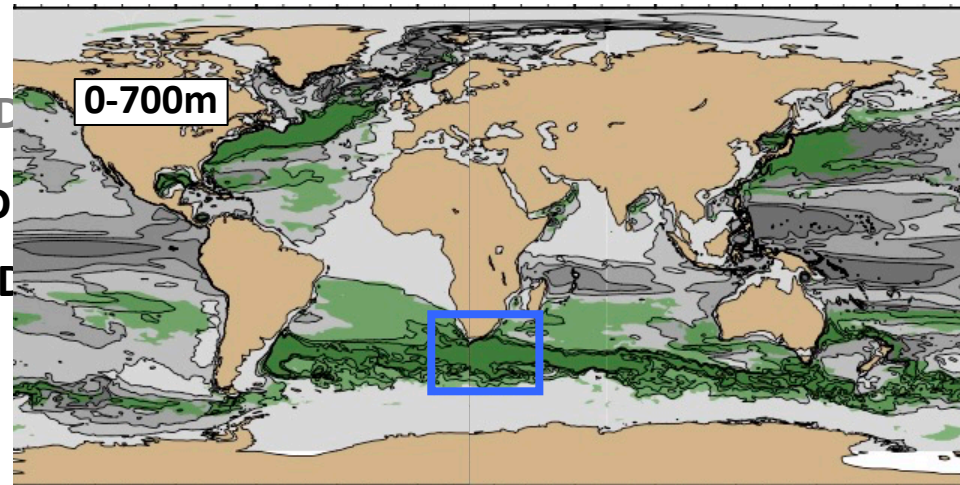
T_{mean} (E_{std})



Chaotic STD

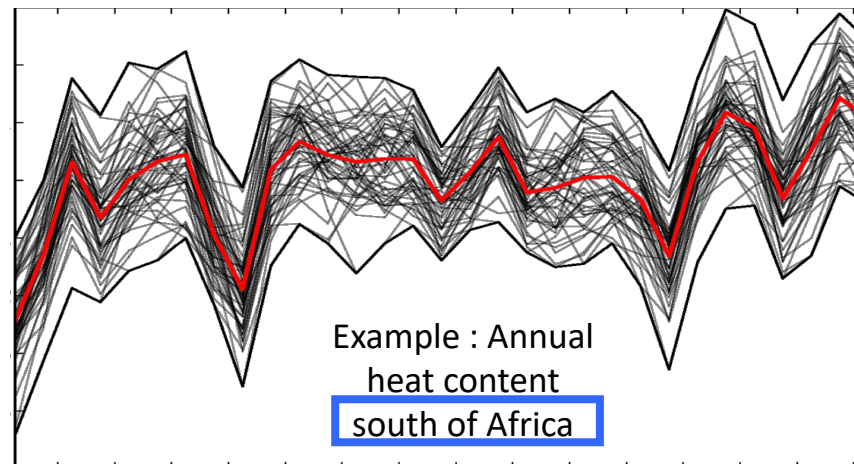
Green:
Chaotic
exceeds
Forced

*Limited
Potential
Predictability*



1980

2010

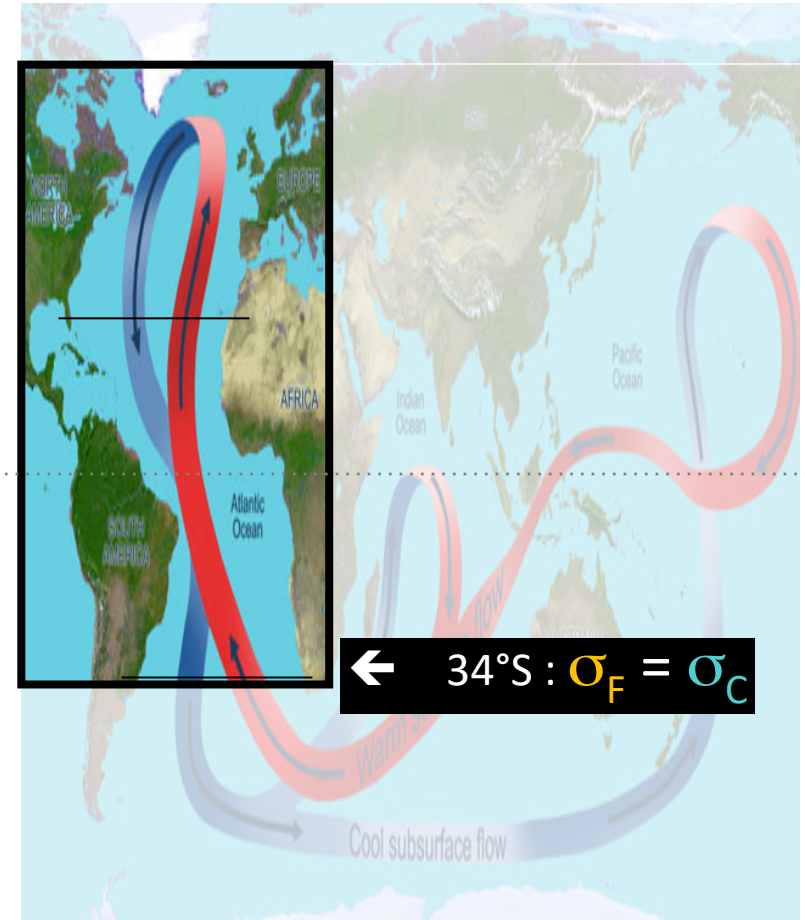
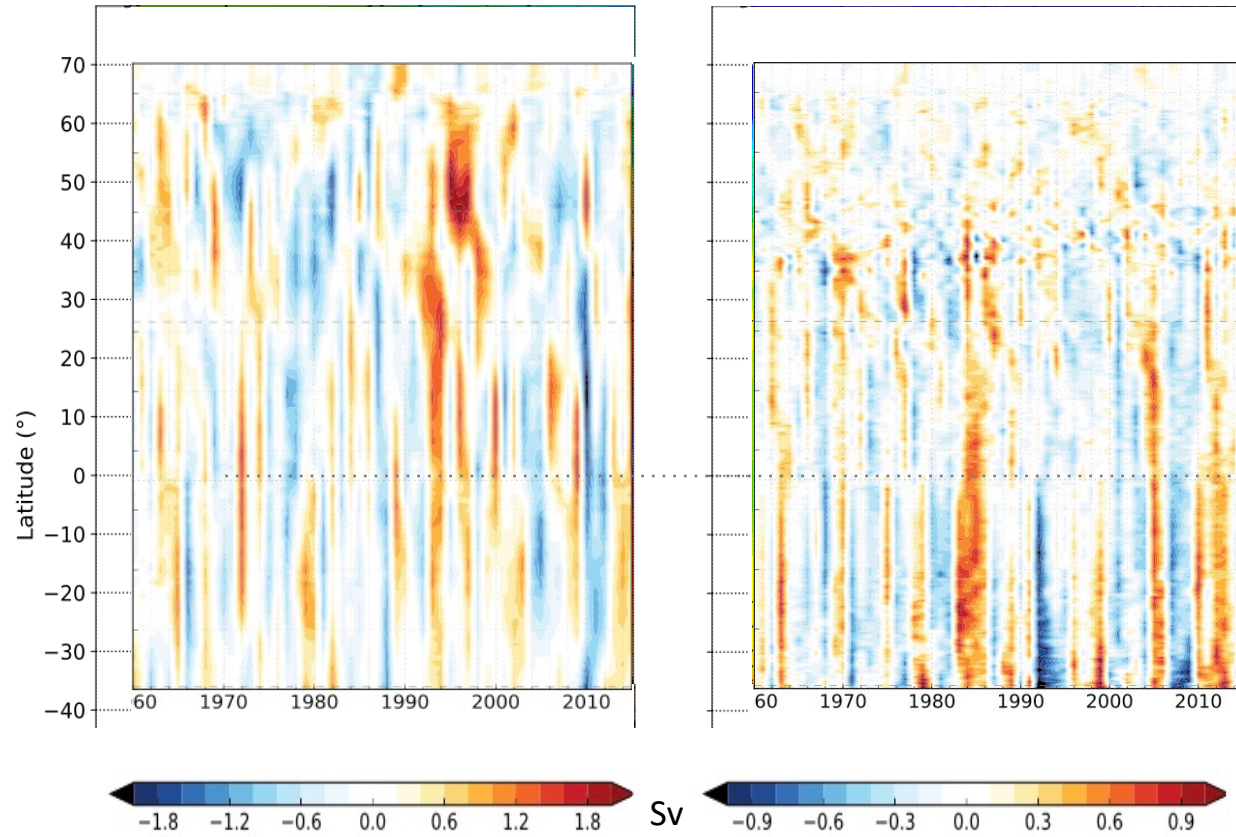


Atlantic MOC : yearly hovmoellers

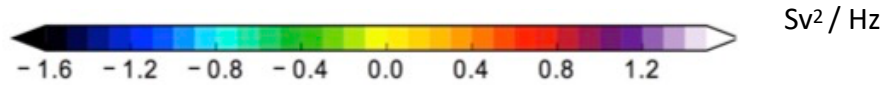
Member 5
Total variability

FORCED

CHAOTIC

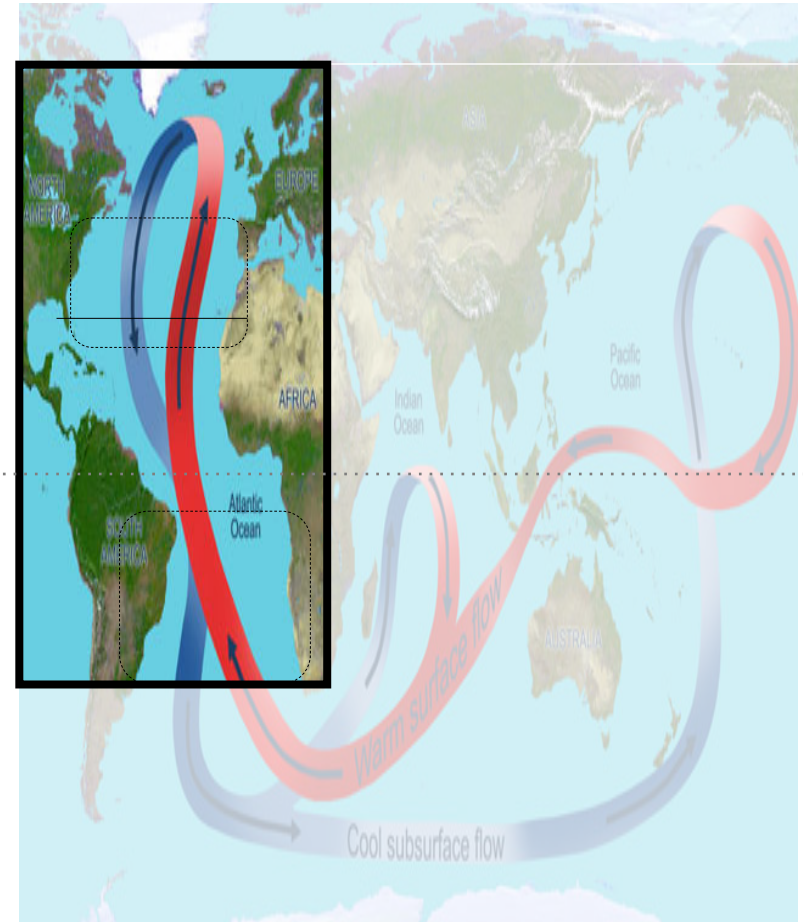
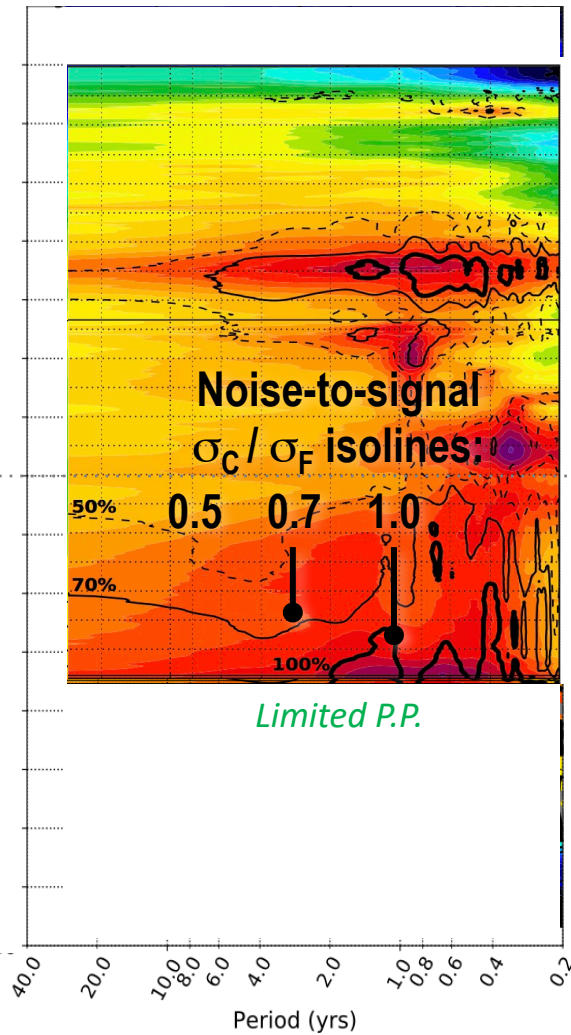
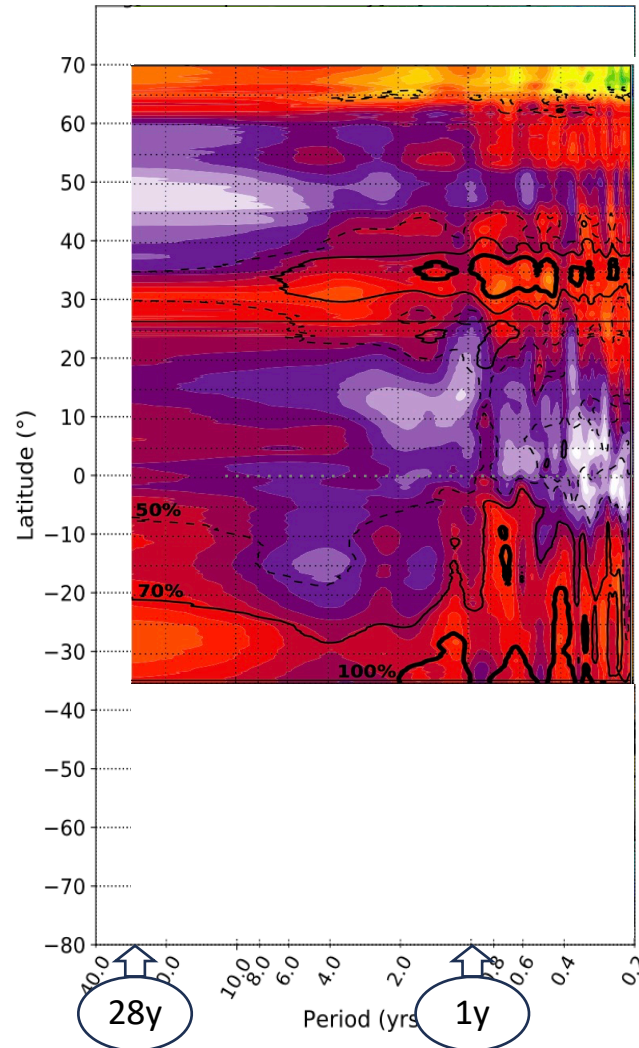


Atlantic MOC : spectra

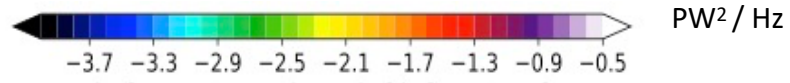


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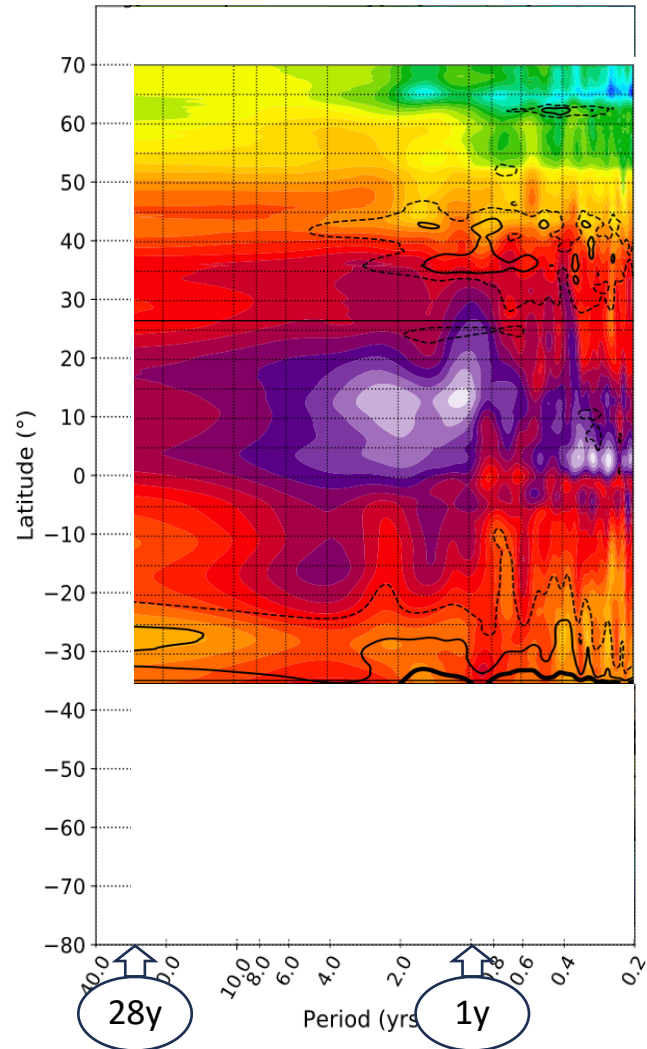
CHAOTIC



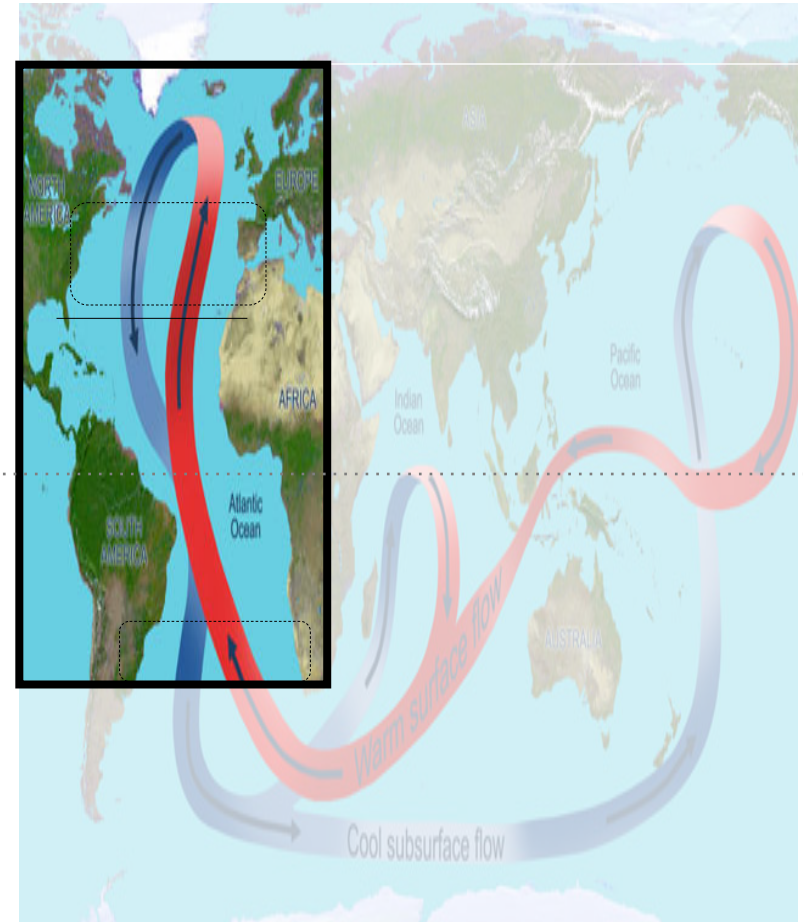
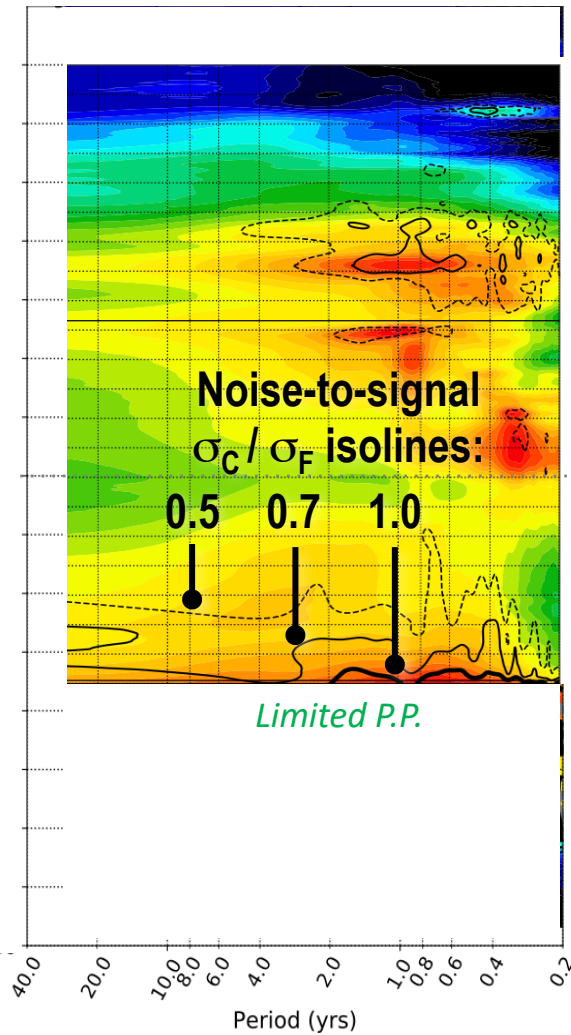
Atlantic MHT : spectra



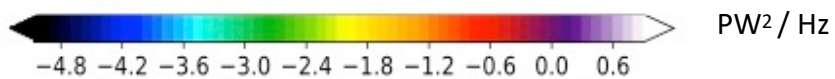
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CHAOTIC

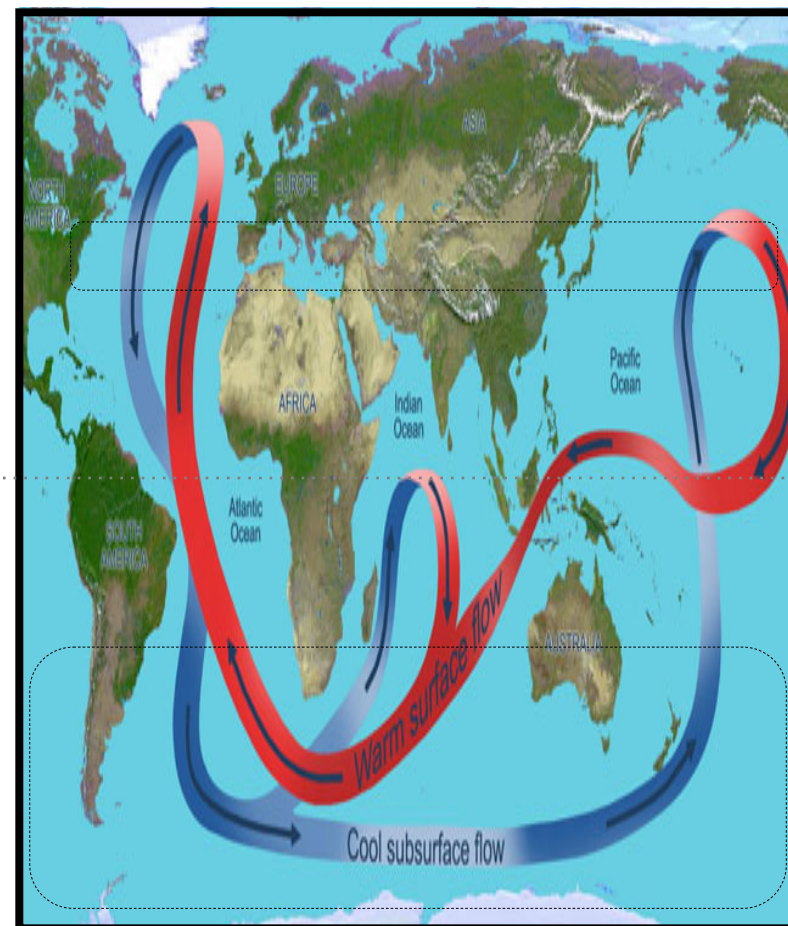
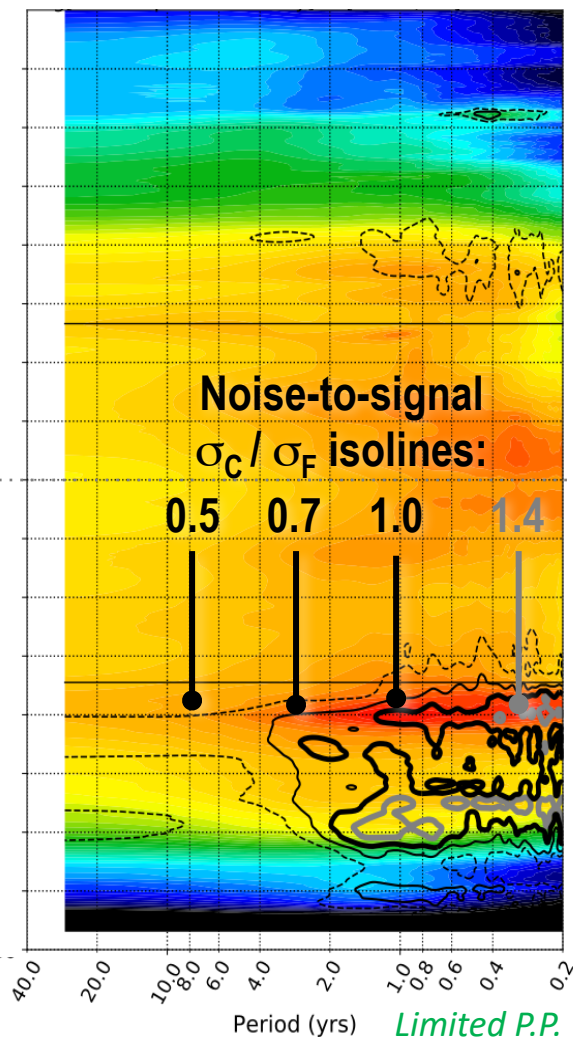
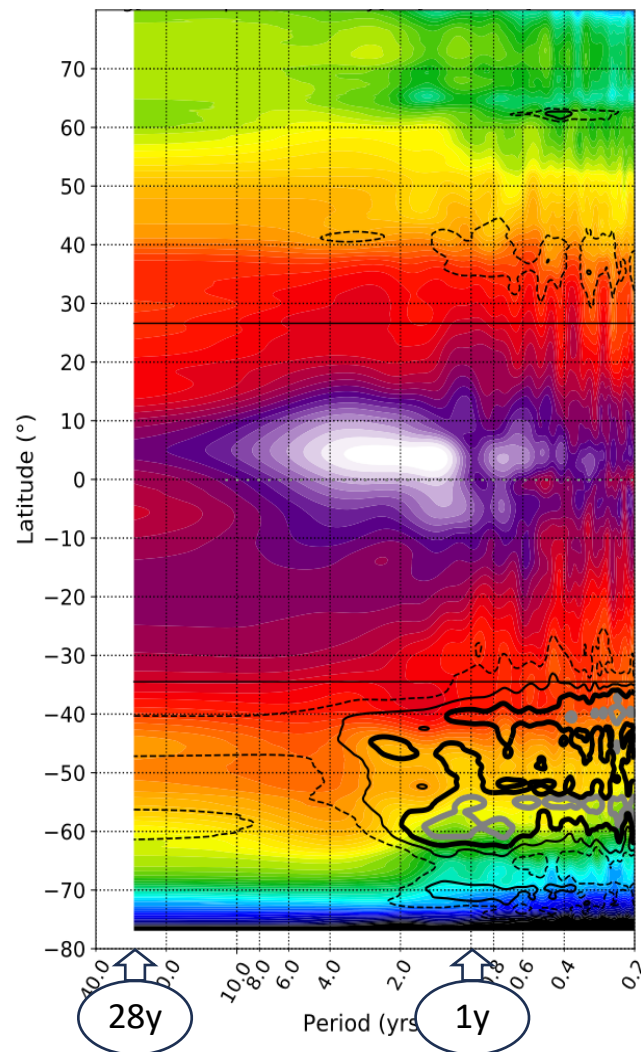


Global MHT : spectra



FORCED

CHAOTIC

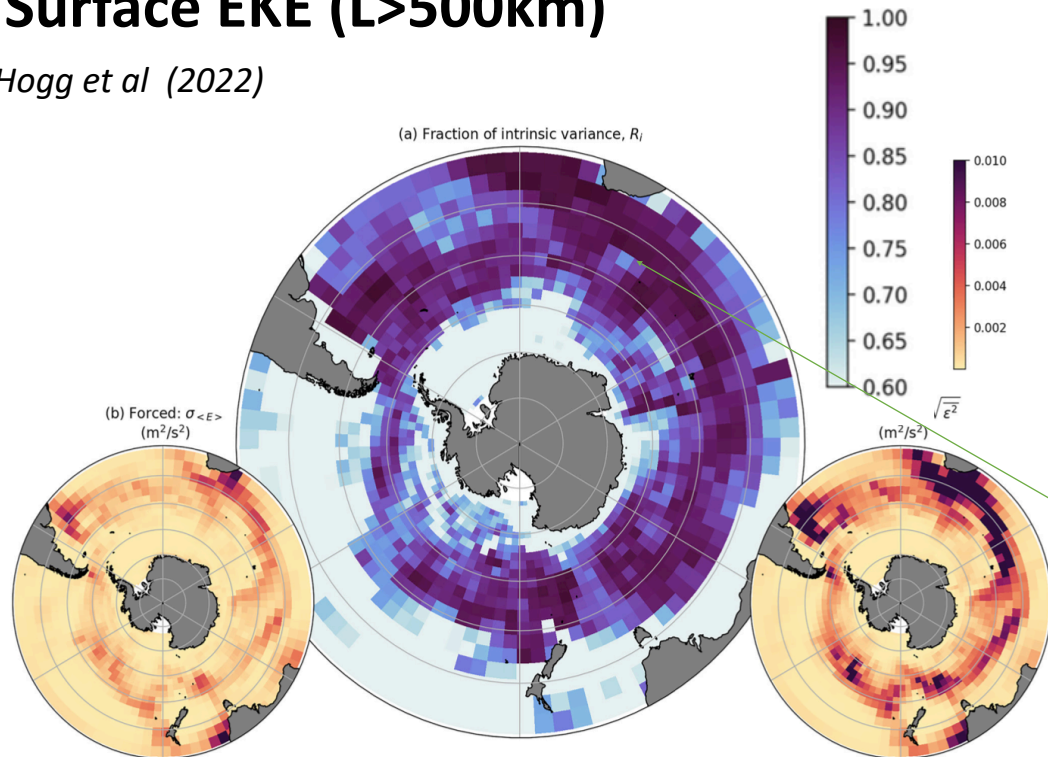


Other indices: Forced & Chaotic 2-18 yr variance ratios

$$\frac{\sigma_C^2}{\sigma_T^2}$$

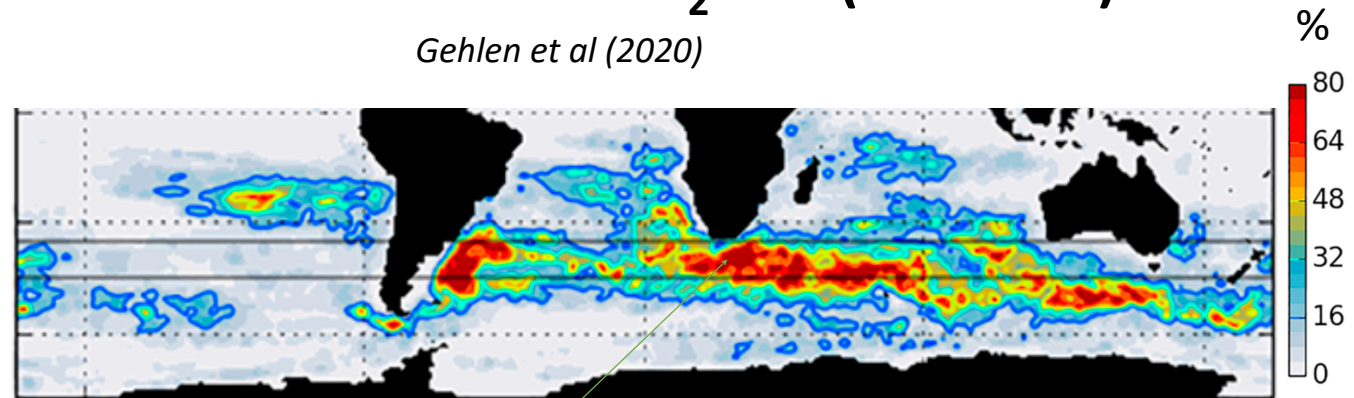
Surface EKE (L>500km)

Hogg et al (2022)



Air-sea CO₂ flux (L>500km)

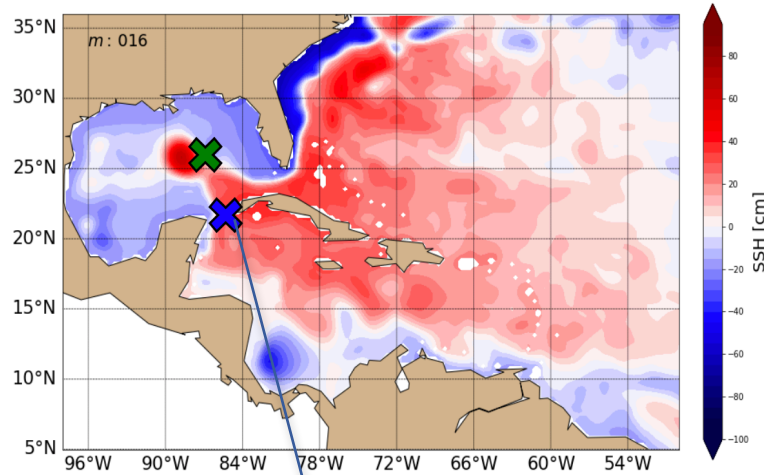
Gehlen et al (2020)



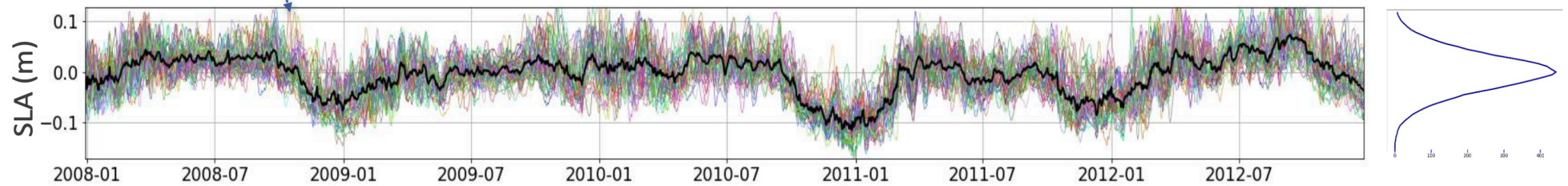
Limited P.P.

OK. But can we separate CIV and forced variability?

[daily] SSH



Reasonable

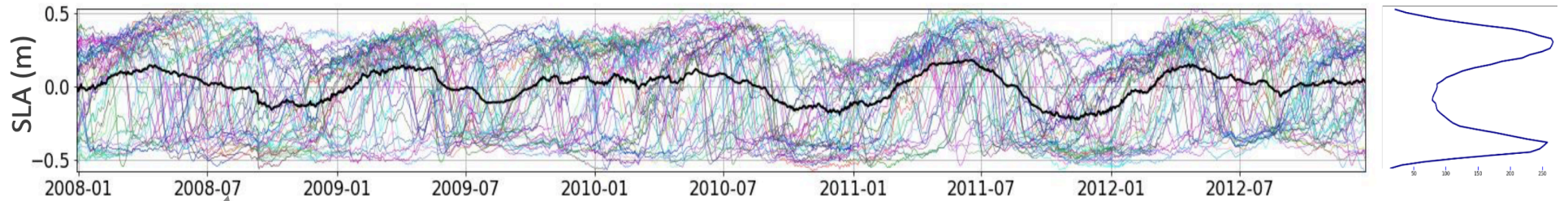


Gaussian e-PDFS : E-mean & E-std are sufficient

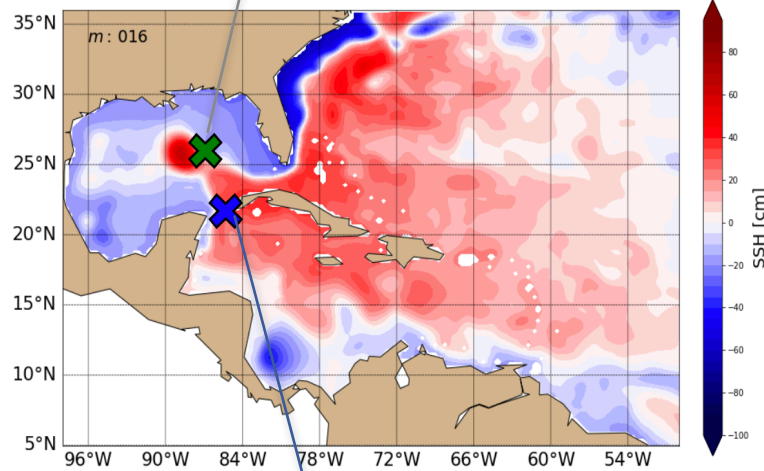
→ *Variability ~ deterministic signal + gaussian noise*

OK. But can we separate CIV and forced variability?

Questionable



[daily] SSH

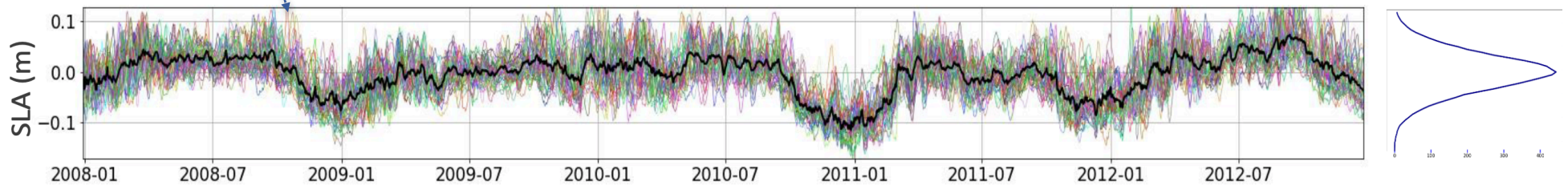


Non Gaussian : E-mean & E-std are not sufficient

→ **Non-autonomous Dynamical Systems**

The atmosphere modulates the oceanic « chaos »

Reasonable



Gaussian e-PDFS : E-mean & E-std are sufficient

→ **Variability ~ deterministic signal + gaussian noise**

II.

No Forced / chaotic separation:

Non-autonomous DS viewpoint

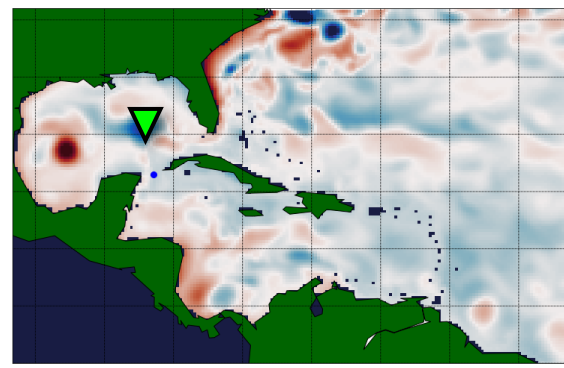
1. Analog predictability

Non-autonomous DS
Fully-variable forcing

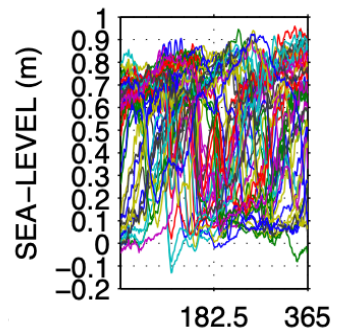
Boer 2000 (attempt)

50 members
x 9 years (2004-2012)
= 450 one-year daily
timeseries of sea level η

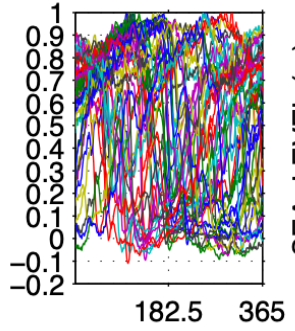
[daily] SSH in the Loop Current



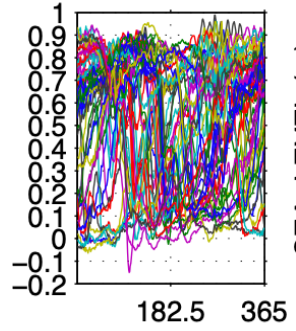
15-day LC predictability?
Dependance on:
- Initial state
- Initial day



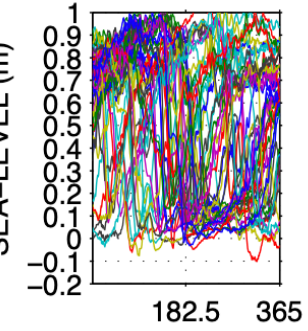
2004



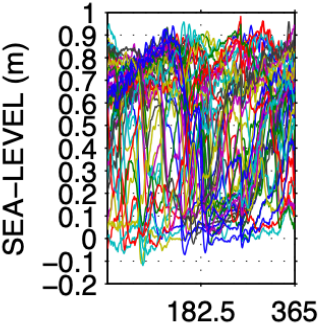
2005



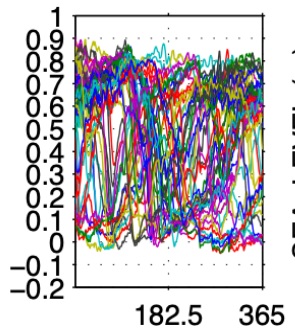
2006



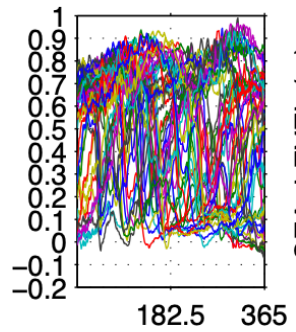
2007



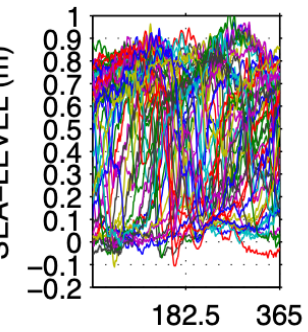
2008



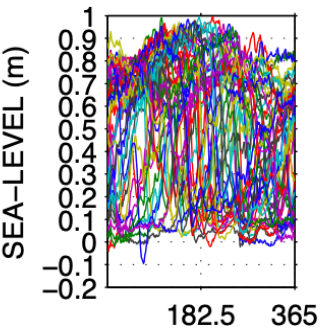
2009



2010



2011



2012

1. Analog predictability

Non-autonomous DS
Fully-variable forcing

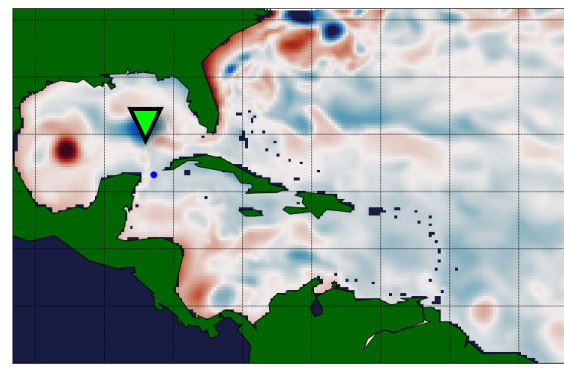
Boer 2000 (attempt)

15-day shift

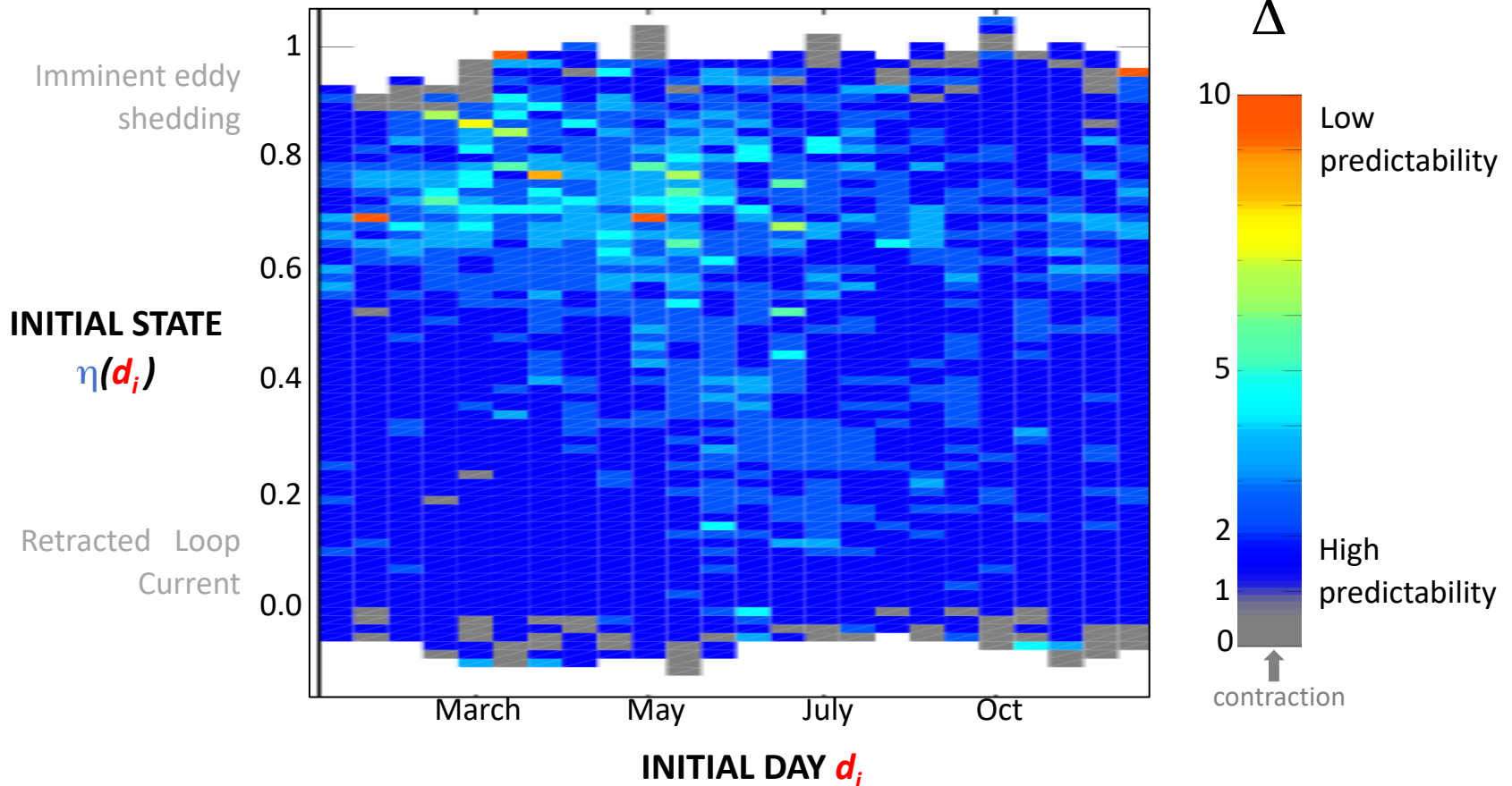
- 15-day period within each year : $d_i \dots d_i+15$
- 50 x 9 = 450 sea level timeseries : $\eta(d_i) \dots \eta(d_i+15)$
- Sort and bin all time series by initial state $\eta(d_i)$
- 15-day separation factor Δ between initially close members

$$\Delta(d_i, \eta(d_i)) = \left\langle \frac{\delta(d_i + 15)}{\delta(d_i)} \right\rangle_{Pairs}$$

[daily] SSH in the Loop Current

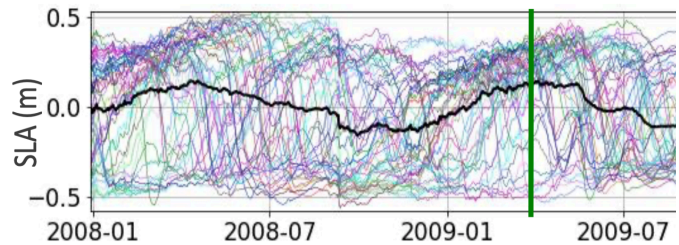


15-day LC predictability?
Dependance on:
- Initial state
- Initial day

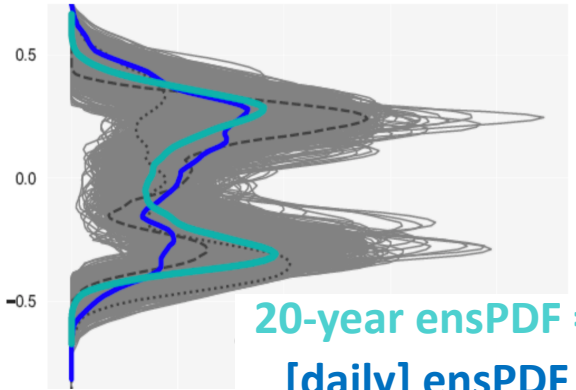


2. Forcing modulates chaotic attractor

Non-autonomous DS
Fully-variable forcing



[daily] SSH in the Loop Current



20-year ensPDF = Q
[daily] ensPDF = P

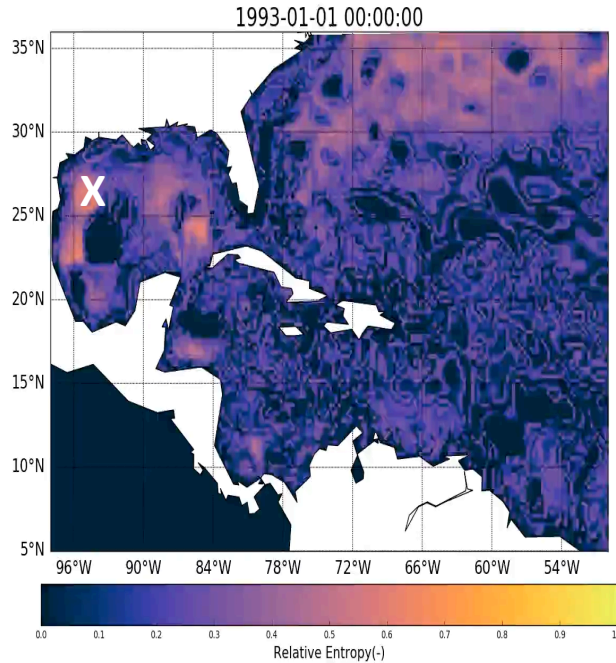
Deciles : N=10

$$E_{ref}(x, y) = - \sum_{i=1}^N Q_i \ln(Q_i)$$

$$E_{daily}(x, y, t) = - \sum_{i=1}^N P_i \ln(P_i)$$

$$[daily] S(x, y, t) = \frac{E_{daily}}{E_{ref}}$$

Normalized entropy S :
[daily] atmospheric
constraint on the
oceanic chaos

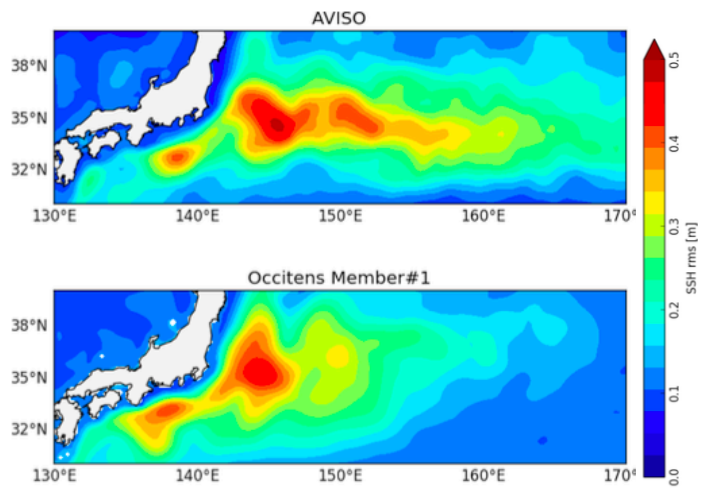
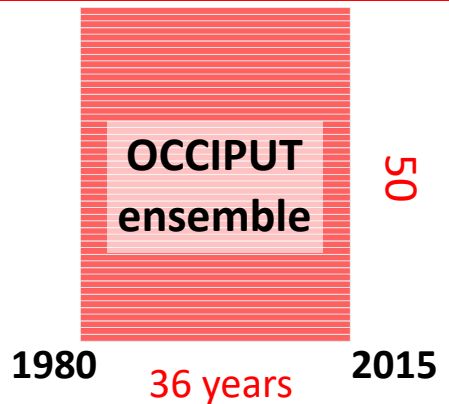


S=0
Strong constraint

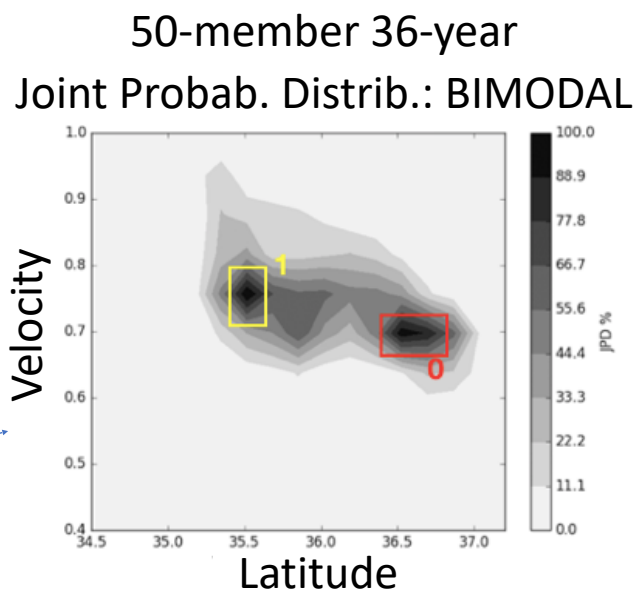
S=1
Weak constraint

3. Forcing modulates chaotic attractor in phase space

Non-autonomous DS
Fully-variable forcing

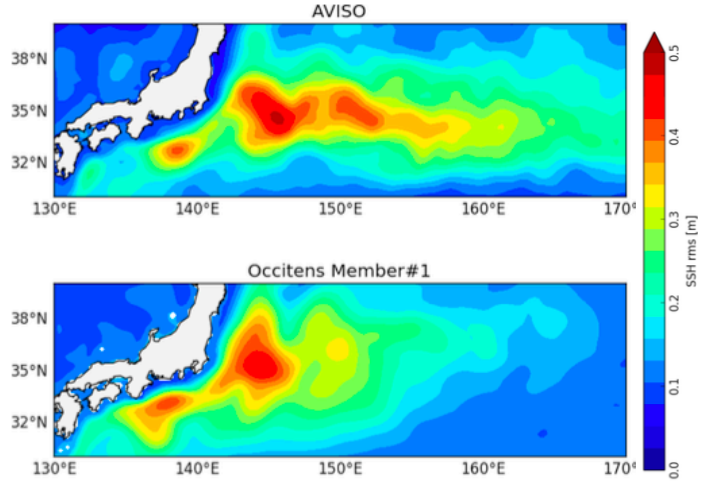
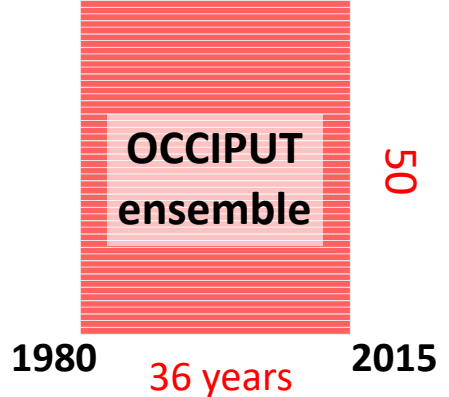


Kuroshio Velocity: $Vel(\text{time}, \text{member})$
Latitude: $Lat(\text{time}, \text{member})$



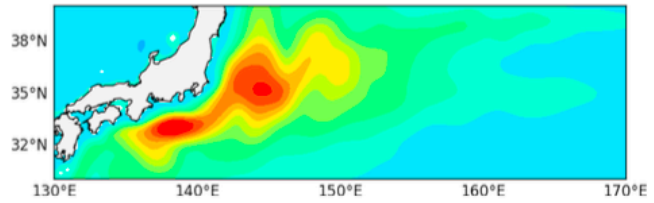
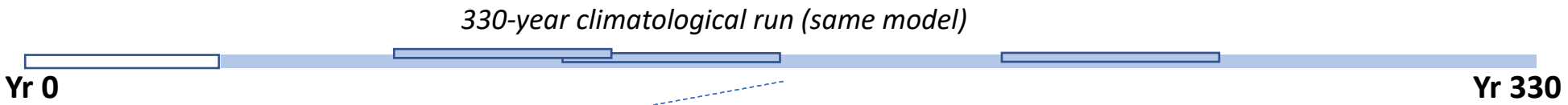
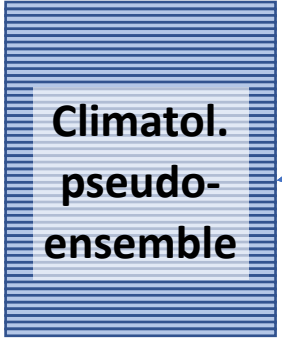
3. Forcing modulates chaotic attractor in phase space

Non-autonomous DS
Fully-variable forcing



Kuroshio Velocity: $Vel(\text{time}, \text{member})$
Latitude: $Lat(\text{time}, \text{member})$

Quasi-autonomous DS
Climatological forcing



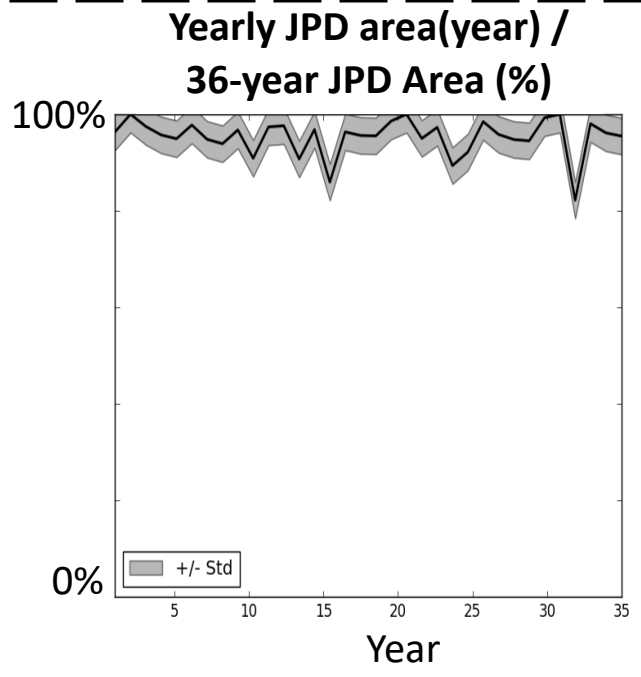
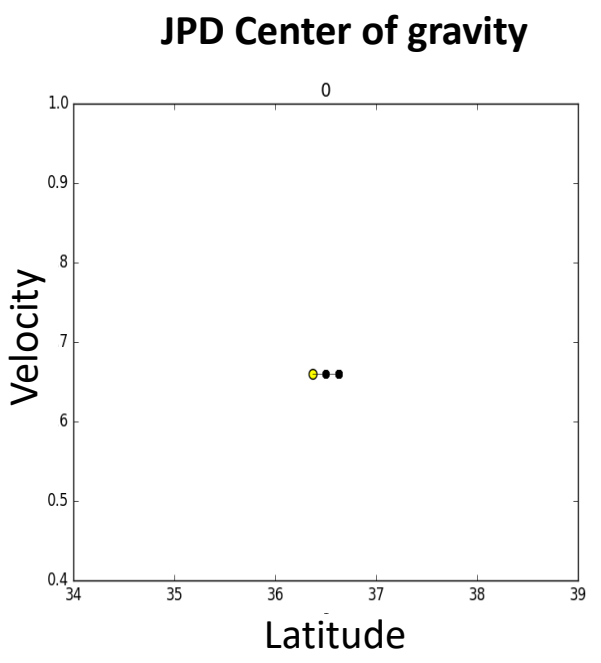
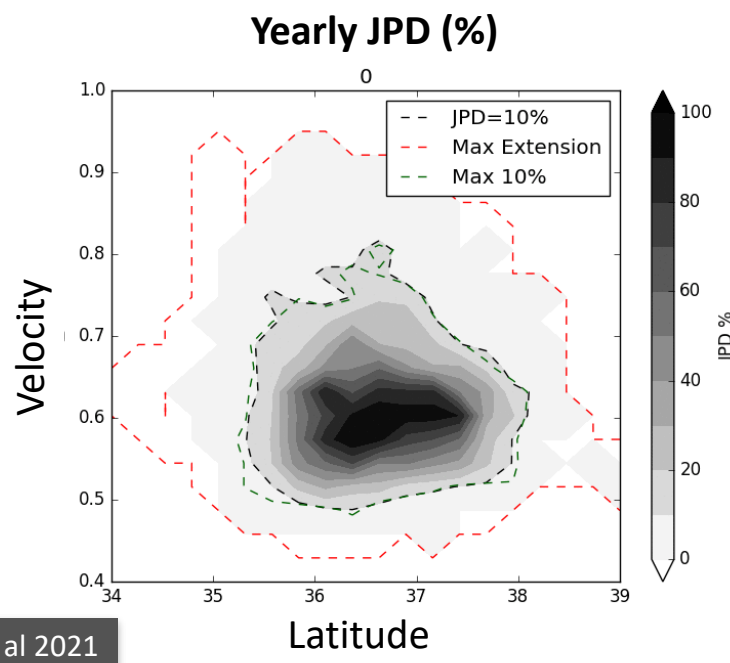
3. Forcing modulates chaotic attractor in phase space

Non-autonomous DS
Fully-variable forcing

Quasi-autonomous DS
Climatological forcing

System's attractor is barely affected by (cyclo) stationary forcing

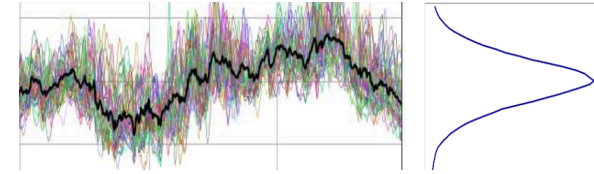
Fedele et al 2021



Conclusion: ocean variability (& predictability)

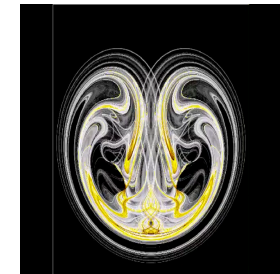
= **Forced variability** + **CIV (in the non linear regime)** → Separation?

- Simple. Classical (e.g. IPCC). OK if gaussian E-PDFs
- **CIV** affects most ocean climate indices (up to basin-scale, up to 100 years)
- **CIV** locally > **forced variability** → reduces potential predictability



= **Atmospherically-modulated CIV**

- **Atmosphere** modulates the **ocean's chaotic attractor**
- Valid if Gaussian or not. More rigorous (DST) → predictability, bifurcations...
- Challenging (OGCM size) but promising (understand dynamics, interpret obs.)



Lorenz
Random
attractor
(Chekroun
et al, 2011)

OCCIPUT papers : <https://meom-group.github.io/projects/occiput/>

OCCIPUT outputs : Thierry.Penduff@cnr.fr

Absent tomorrow :
glad to chat on Wednesday